## Enfield Local Authority Written Calculation Policy 2014


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## Enfield LA Calculation Policy 2014

The following calculation policy has been devised to meet requirements of the National Curriculum 2014 for the teaching and learning of mathematics, and is also designed to give pupils a consistent and smooth progression of learning in calculations across the school.
Enfield LA Maths Team will be working with Early Years Consultants to produce maths guidance for nursery and reception.

## Age stage expectations

The calculation policy is organised according to age stage expectations as set out in the National Curriculum 2014, however it is vital that pupils are taught according to the stage that they are currently working at, being moved onto the next stage once they show conceptual understanding, or working at a lower stage until they are secure enough to move on.

## Providing a context for calculation:

It is important that any type of calculation is given a real life context or problem solving approach to help build children's understanding of the purpose of calculation, and to help them recognise when to usecertain operations and methods when faced with problems. This mustbe a priority within calculation lessons.

## Choosing a calculation method:

Children need to be taught and encouraged to use the following processes in deciding what approach they will take to a calculation, to ensure they select the most appropriate method for the numbers involved:


| To work out a tricky <br> calculation: |
| :---: |
| Approximate |
| Calculate |
| Check |

## Key Stage 1 - Addition



Terry has 3 apples and Tony has 2 apples. How many altogether?

- Number lines to 20.

- Derive related facts to 20 .

$$
\begin{aligned}
& \square=5+4 \\
& 5+4=\square \\
& \square+4=9 \\
& \square+\square=9
\end{aligned}
$$



- Money and addition up to 20p.

- Read, write and interpret mathematical statement involving addition (+) and equals ( $=$ ).


## Video clips:

Using a range of equipment and strategies to reinforce addition statements

## National Curriculum requirements:

Add 1 digit and 2 digit numbers to 20 , including 0 .

## Y2

Through practical activities in meaningful contexts and informal written methods.

- Fluent recall of bonds to 20 and within 20.
- Derive and use related facts up to 100 .
- Addition of money up to $£ 1$.

- Add numbers using concrete objects, pictorial representations and mentally.

- Show that addition of two numbers can be done in any order (commutative).
- Recognise and use the inverse relationship between addition and subtraction.
- Progressing to partitioned columnar method (in preparation for year 3).



## National Curriculum requirements:

(using concrete objects, pictorial representations and mentally)
Add 2 digit numbers and ones.
Add 2 digit number and tens.
Add two 2 digit numbers.
Add three 1 digit numbers.

## Key Stage 2 - Addition

## Y3

- Continue with partitioned columnar method.
- Introduce expanded columnar addition.


Progressing to the compact columnar method.

| T O | H T O | T O | H T O | T O | H T O |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 23 | 315 | 94 | 561 | 47 | 237 |
| + 42 | +624 | + 73 | + 718 | $+25$ | + 516 |
| 65 | 939 | 167 | 1279 | 72 | 753 |
|  |  |  |  | 1 | 1 |

- Add money using both $£$ and pence in practical contexts.


## Video clip:

Demonstration of expanded 3 digit columnar addition

## National Curriculum requirements:

Add numbers with up to 3 digits, using the formal written method of columnar addition.

- Continue with columnar addition.

| + | H T O | + | H T O | + | Th H T O |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 371 |  | 376 |  | 2388 |
|  | 485 |  | 485 |  | 1124 |
|  | 856 |  | 861 |  | 3512 |
|  | 1 |  | 11 |  | 11 |

- Estimate and use inverse operations to check answers to a calculation.
- Add money using both $£$ and pence in practical contexts.


## National Curriculum requirements:

Add numbers with up to 4 digits, using the formal written method of columnar addition.

## Key Stage 2 - Addition

- Continue to use columnar addition, adding numbers with more than 4 digits.

$$
\begin{array}{r}
32879 \\
+\quad 3987 \\
\hline 68866 \\
\hline
\end{array}
$$

- Addition of money and decimals.



## National Curriculum requirements:

Add whole numbers with more than 4 digits, using the formal written method of columnar addition.

## Y6

- Add several numbers of increasing complexity using columnar addition.



## National Curriculum requirements:

Add whole numbers with more than 4 digits, using the formal written method of columnar addition.

## Key Stage 1 - Subtraction



- Represent and use number bonds within 20.
- Record using subtraction (-) and equals signs (=)
- Derive related facts up to 20 .

| $5-2=\square$ | $\square=5-2$ |
| :--- | :--- |
| $5-\square=3$ | $3=\square-2$ |
| $\square-2=3$ | $3=5-\square$ |
| $\square-\square=3$ | $3=\square-\square$ |



- Counting back on a 100 square and a vertical number line.


## National Curriculum requirements:

Subtract 1 digit and 2 digit numbers up to 20 , including 0 .
Represent and use number bonds and related subtraction facts.

## Y2

Through practical and meaningful contexts.

- Fluent recall of bonds to 20 and within 20 .
- Derive and use related facts up to 100 e.g. $10-7=3$ so $100-70=30$.
- Counting back by partitioning second number. Subtract the ones first to be in line with columnar subtraction
E.g. 46-18 46-10-8

- Find the difference by counting up (only when the difference is small). $23-18=5$

- Recognise and use the inverse relationship between addition and subtraction
- Show that subtraction is not commutative (done in any order)
- Progressing to the partitioned columnar method in preparation for year 3
- Subtraction of money, including change.


## National Curriculum requirements:

(using concrete objects, pictorial representations and mentally)
Subtract 2 digit numbers and ones.
Subtract 2 digit number and tens.
Subtract two 2 digit numbers.
Subtract three 1 digit numbers.

Key Stage 2 - Subtraction

- Continue with vertical number line subtraction progressing to the expanded columnar subtraction method.


## $89-35=54$

$$
80+9
$$

$$
-30+5
$$

$$
50+4=54
$$

- Introduce exchanging through the expanded columnar subtraction method.
72-47


$$
\begin{aligned}
& 6020+{ }^{1} 2 \\
& -\underline{40+7} \\
& \underline{20+5}=25
\end{aligned}
$$

- Progressing on to compact columnar subtraction.

| TO | H TO | TO |
| ---: | ---: | ---: |
| 47 | 864 | $45^{1} 1$ |
| -23 | $\underline{-621}$ | $\underline{-36}$ |
| 24 | $\underline{243}$ | $\underline{15}$ |

- Emphasise value of digit, e.g. 4 tens subtract 2 tens $=2$ tens. Use the correct language for subtraction i.e. exchange rather than borrow.
- Subtract amounts of money to give change.


## Video clips:

Subtraction - teaching children to consider the most appropriate methods before calculating

Introducing partitioned column subtraction method, from practical to written

## National Curriculum requirements:

Subtract numbers with up to 3 digits using the formal written method of columnar subtraction.

- Continue with partitioned columnar subtraction progressing to compact columnar subtraction.

| H T O | H T O | H T O | Th H T O |
| :---: | :---: | :---: | :---: |
| ${ }^{3} 437$ | ${ }^{3} 4^{12} \not 8^{1} 2$ | ${ }^{5} \phi^{9 \%} \chi^{1}{ }^{1} 4$ | $8{ }^{3} 4^{11} \not 2^{1} 6$ |
| -182 | -187 | - 347 | -2177 |
| 255 | 245 | 3 5 7 | 6249 |

- Estimate and use inverse operations to check answers to a calculation.
- Subtract amounts of money using columnar method.


## Video clips:

Subtraction - teaching children to consider the most appropriate methods before calculating

Introducing partitioned column subtraction method, from practical to written

Moving to the compact column method of subtraction

## National Curriculum requirements:

Subtract numbers up to 4 digits using the formal written method of columnar subtraction.

## Key Stage 2 - Subtraction

## Y5

- Continue with compact columnar subtraction, including subtraction of decimals.

- Use rounding to check answers to calculations and to determine, in the context of a problem, levels of accuracy.


## Video clip:

Moving to the compact column method of subtraction

## National Curriculum requirements:

Subtract numbers with more than 4 digits.

- Continue with compact columnar subtraction, including subtraction of decimals.

- Use estimation to check answers to calculations and to determine, in the context of a problem, levels of accuracy.


## National Curriculum requirements:

Subtract numbers with more than 4 digits.

## Key Stage 1 - Multiplication

Through practical activities and meaningful contexts using concrete objects,
pictorial representations and arrays with the support of the teacher.

- Doubles.
$7+7=14$
- Make connections between arrays, number patterns and counting in 2's, 5 's to 50 and 10 's to 100.
- Use of number lines.

- "100 Square" to count in 2's, 5's and 10's.

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |

- There are 2 sweets in one bag. How many sweets are there in 5 bags?

- Counting multiples of coins: $2 p, 5 p, 10 p$.



## National Curriculum requirements:

Solve one step problems involving multiplication, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.

Through practical activities and meaningful contexts using concrete objects, pictorial representations and arrays.

- Double numbers (by partitioning and recombining) $17+17$.


- Understand multiplication as repeated addition/groups/lots.
- Read arrays.


$$
2 \times 4 \text { (2, } 4 \text { times) }
$$

- Repeated addition on a number line.
$2+2+2+2$ (4 groups of 2, 2 four times, $2 \times 4$ )

- Know the multiplication tables for 2,5 and 10.
- Calculate mathematical statements within the multiplication tables using the multiplication (x) and equals (=) signs.
- Show that the multiplication of two numbers can be done in any order (commutative).

Video clips: Teaching for understanding of multiplication facts Practical multiplication and the commutative law

## National Curriculum requirements:

Solve problems involving multiplication using materials, arrays, mental methods and multiplication facts.

## Key Stage 2 - Multiplication

## Y3

## Y4

- Recall and use multiplication tables for 3,4 and 8 .
- Continue to use arrays and number lines/Cuisenaire rods for 3,4 and 8 multiplication tables.
- Write and calculate mathematical statements for multiplication. Statements to include the multiplication tables that they know and 2 digit numbers $\times 1$ digit numbers. Pupils use mental methods and progress to formal written methods.
(grid method removed)
- Progressing to expanded method of multiplication.

| TO |
| ---: |
| 14 |
| $\times \quad 5$ |
| 20 |
| $+\frac{5}{7} 0$ |$(5 \times 4)$

Video clips: Teaching the grid method as an interim step (Partitioning and counters to introduce grid).

National Curriculum requirements: Multiply 2 digits by 1 digit, using mental and progressing to formal written methods.

- Recall and use multiplication tables up to $12 \times 12$ (Including multiplying by 0 and 1 ).
- Short Multiplication.


| No carrying | Extra digit | Carrying | Zeros | Ext. |
| :---: | :---: | :---: | :---: | :---: |
| T O | H T O | H T O | H T O | H T O |
| 32 | 51 | 38 | 202 | $\square 5 \square$ |
| x $\frac{3}{\underline{96}}$ | $\mathrm{x} \frac{2}{102}$ | $\mathrm{x} \frac{7}{266}$ | $\mathrm{x} \frac{4}{808}$ | $\mathrm{x} \frac{4}{\frac{612}{5}}$ |
|  |  | $\underline{21}$ |  |  |

## National Curriculum requirements:

Multiply 2 digits by 1 digit using formal written layout. Multiply 3 digits by 1 digit using formal written layout.

- Recall and use multiplication tables up to $12 \times 12$ (Including multiplying by 0 and 1 ).
- Continue to practise short multiplication.
- Use Grid Method to introduce long multiplication.



## Video clips:

Moving from grid method to a compact method
Reinforcing rapid times table recall
Demonstration of long multiplication

## National Curriculum requirements:

Multiply numbers up to 4 digits by a 1 digit number using the formal written method of short multiplication.

Multiply numbers up to 4 digits by a 2 digit number using the formal written method of long multiplication.

Multiple whole numbers and those involving decimals by $10,100,1000$.

- Recall and use multiplication tables up to $12 \times 12$ (Including multiplying by 0 and 1 ).
- Continue to practise short multiplication.
- Continue to practise long multiplication.

- Multiply decimals using the grid method and progressing on to short multiplication.
- Use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy.


## Video clips:

Moving from grid method to a compact method
Reinforcing rapid times table recall
Demonstration of long multiplication

## National Curriculum requirements:

Multiply up to 4 digits by 2 digits using the formal written method of long multiplication.
Multiply numbers by $10,100,1000$ giving answers up to 3 decimal places.

## Key Stage 1 - Division

|  |
| :--- |
| Through practical activities in meaningful contexts. |
| - Division as sharing. |
| Emphasise the importance of sharing equally. |
| Share a bag of 15 sweets between 5 children - one for you, one for you, |
| one for you, one for you, one for me. |



12 shared between 3 is 4


- Introduce halving even numbers up to 10 .


## Half of 4



## National Curriculum requirements:

Solve one step problems involving division, by calculating the answer by using concrete objects, pictorial representations and arrays with the support of the teacher.

Through practical activities in meaningful contexts.

- Recall and use division facts for 2,5 and 10 times tables.
- Continue to use division as sharing.
- Division as grouping.
- 15 children get into teams of 5 to play a game. How many teams are there?


How many groups of 5 in 15 ?
How many 5's have been counted?


How many 2's in 10 ?

- Understand ' $\div 2$ ' as 'half of'.
- Understand that division is not commutative.
- Recognise relationship between x and $\div$
- Record using division ( $\div$ ) and equals (=) signs.
- Use number lines to answer questions such as $20 \div 2=$
 l11111111111111111111


## National Curriculum requirements:

Solve problems involving division using materials, mental methods and division facts.

## Key Stage 2 - Division

## Y3

- Recall and use division facts for 3,4 , and 8 times tables.
- Write and calculate mathematical statements for division using the tables they know.
- Introduce short division, with exact answers.

- Progressing to short division involving carrying, with exact answers.


## National Curriculum requirements:

Division questions based on multiplication tables they know.
Divide 2 digits by 1 digit, progressing to formal written methods.
The National Curriculum statutory requirements for Year 3 and the use of written methods are not clear therefore our guidance for Year 3 has been based on the skills required to access Year 4 statutory requirements.

## Y4

- Recall and use all division facts for all tables up to 12 (Including dividing by 1 ).
- Continue with short division method.

$$
4 \longdiv { 1 8 } \quad \frac { 0 3 7 } { 5 \longdiv { 1 8 ^ { 3 } 5 } } \quad \frac { 2 1 8 } { 4 \longdiv { 8 7 ^ { 3 } 2 } }
$$

- Progressing to short division with remainders.



## National Curriculum requirements:

Divide 2 digits by 1 digit and 3 digits by 1 digit becoming fluent with formal written method of short division with exact answers and progressing to remainders.

The National Curriculum statutory requirements for Year 4 and the use of written methods are not clear therefore our guidance for Year 4 has been based on the skills required to access Year 5 statutory requirements.

## Key Stage 2 - Division

## Y5

- Consolidate the use of the formal written method of short division.
- 



- Introduce long division
$432 \div 15$ becomes

Answer: 28 remainder 12
$432 \div 15$ becomes

$$
\begin{aligned}
& \frac{12}{15}=\frac{4}{5} \\
& \text { Answer: } 28 \frac{4}{5}
\end{aligned}
$$

$$
432 \div 15 \text { becomes }
$$

Answer: 28.8

## National Curriculum requirements:

Divide 2 digits by 1 digit.
Divide 3 digits by 1 digit.
Divide 4 digits by 1 digit.
Children interpret the remainders appropriately for the context.
e.g. as fractions, decimals or by rounding
$98 \div 4=98 / 4=24 \mathrm{r} 2=241 / 2=24.5$ rounded to 25
Divide whole numbers and those involving decimals by $10,100,1000$.

## Y6

- Consolidate short division.
- Children should be able to interpret remainders as whole number remainders, fractions or by rounding, as appropriate for the context.

$$
\begin{gathered}
98 \div 7 \text { becomes } \\
\begin{array}{c}
1 \quad 4 \\
7 \begin{array}{|cc|}
\hline 2 \\
9
\end{array}
\end{array}
\end{gathered}
$$

- Answer: 14


Answer: 86 remainder 2
$496 \div 11$ becomes

N.B: The above examples are taken from the National Curriculum for Mathematics appendix.

## National Curriculum requirements:

Divide numbers up to 4 digits by a 2 digit number using the formal written method of short division where appropriate.

Divide up to 4 digits by a 2 digits whole number using the formal written method of long division.

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